

Geometria Diferencial de Curvas

1	Triedro de Frenet–Serret	$\vec{T}(t) = \frac{\vec{r}'(t)}{ \vec{r}'(t) }$ $\vec{N}(t) = \frac{\vec{T}'(t)}{ \vec{T}'(t) }$ $\vec{B}(t) = \vec{T}(t) \times \vec{N}(t)$
2	Curvatura	$\kappa(t) = \frac{ \vec{T}'(t) }{ \vec{r}'(t) } = \frac{ \vec{r}'(t) \times \vec{r}''(t) }{ \vec{r}'(t) ^3}$
3	Raio de curvatura	$\rho(t) = \frac{1}{\kappa(t)}$
4	Torção	$\tau(t) = \frac{ \vec{B}'(t) }{ \vec{r}'(t) }$

Operador $\vec{\nabla}$

1	Gradiente	$\vec{\nabla} f = \left(\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z} \right)$
2	Divergente	$\operatorname{div} \vec{F} = \vec{\nabla} \cdot \vec{F} = \frac{\partial F_1}{\partial x} + \frac{\partial F_2}{\partial y} + \frac{\partial F_3}{\partial z}$
3	Rotacional	$\operatorname{rot} \vec{F} = \vec{\nabla} \times \vec{F} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ \partial/\partial x & \partial/\partial y & \partial/\partial z \\ F_1 & F_2 & F_3 \end{vmatrix}$
2	Laplaciano	$\Delta f = \vec{\nabla}^2 f = \vec{\nabla} \cdot \vec{\nabla} f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2} + \frac{\partial^2 f}{\partial z^2}$

Teoremas de Green, Stokes e Gauss – Hipóteses omitidas

1	Teorema de Green	$\iint_R \left(\frac{\partial F_2}{\partial x} - \frac{\partial F_1}{\partial y} \right) dx dy = \oint_{\partial R} \vec{F} \cdot d\vec{r}$
2	Teorema de Stokes	$\iint_S \operatorname{rot} \vec{F} \cdot \vec{n} dA = \oint_{\partial S} \vec{F} \cdot d\vec{r}$
3	Teorema da Divergência de Gauss	$\iiint_T \operatorname{div} \vec{F} dx dy dz = \iint_{\partial T} \vec{F} \cdot \vec{n} dA$